



The new developments of matrix and tensor equations

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Abstract

In this talk, I give a brief introduction to some new developments in systems of Sylvester-type matrix equations and tensor equations.

Keywords: Quaternion algebra, matrix equation, rank, Moore-Penrose inverse

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